

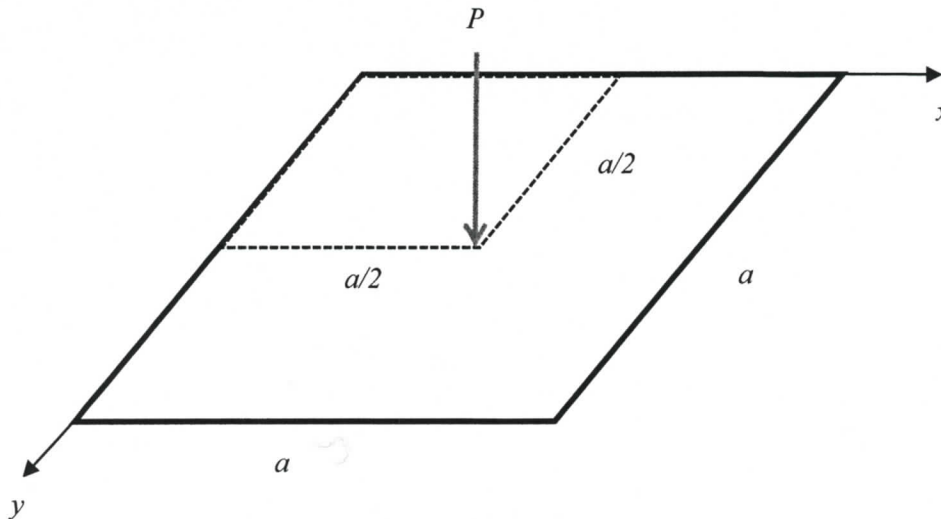
Closed book examination, only writing instruments are allowed. Write your name, study program and the course code on each answering sheet. This exam (2 pages) includes 3 questions (each 8 scores) for 24 scores of the first partial exam. Some of the required formulas are given.

Duration: 2 hours

1. A thin rectangular ($a \times b$) plate is simply supported on all edges and is subjected to the loading $p_z(x, y) = P \sin \frac{2\pi x}{a} \sin \frac{3\pi y}{b}$. Determine the deflection of the plate.

2. A thin circular plate with radius R and flexural rigidity D , is taken to be clamped at the edge and is subjected to rotationally symmetric loading $p_z = \frac{P_0 r^2}{R}$ (r is the variable in the polar coordinate system). Determine the deflection of the plate.

3- Consider a thin clamped square plate ($a \times a$) subjected to a concentrated lateral force P at the center of the plate ($a/2 \times a/2$). The material properties are (E, ν) while the thickness of the plate is h . Determine the deflection of this plate by the Ritz method using one term as the shape function.



Formulas:

Governing equation for the static analysis of classical plate:

$$\nabla^2 \nabla^2 w = \frac{p_z}{D}, \quad D = \frac{Eh^3}{12(1-\nu^2)}$$

Governing equation for the static analysis of axisymmetric circular classical plate in polar coordinates:

$$\nabla^4 w(r) = \frac{p_z(r)}{D}, \quad \text{while} \quad \nabla^4 w = \nabla^2 \nabla^2 w = \frac{1}{r} \frac{d}{dr} \left\{ r \frac{d}{dr} \left[\frac{1}{r} \frac{d}{dr} \left(r \frac{dw}{dr} \right) \right] \right\}$$

In the Kirchhoff-Love model, the potential energy (Π) of a rectangular plate:

$$\Pi = \frac{D}{2} \int_0^b \int_0^a \left\{ (\nabla^2 w)^2 - 2(1-\nu) \left[\frac{\partial^2 w}{\partial x^2} \frac{\partial^2 w}{\partial y^2} - \left(\frac{\partial^2 w}{\partial x \partial y} \right)^2 \right] \right\} dx dy - \int_0^b \int_0^a p_z w dx dy$$

In case of clamped plate, you can use the simplified form of potential energy.