

## February 2016, 2<sup>nd</sup> Exam - Feel free to add to this

### Q1: various definition true/false

... Is Gaussian mixture discriminant?

...Is it possible to determine generalization error with training data?

Can you perform \_\_\_ with unlabelled data?

### Q2: Bayesian Decision Theory & Parametric Methods

Blah blah classifiers, 100 samples of binary data, sorted so that first 50% is 0, second 1. Data is in bins/groups of 25.. something something..

a) What is the version space of the above classifiers?

<Something about posterior, prior, maximum a posteriori>

<Maximum likelihood given  $\sigma^2$ ?>

### Q3: Combining Classifiers

<Description here>... something about 3 classifiers K

a) Explain the advantages of using multiple classifiers and how to combine them.

b) List 4 methods to make classifiers diverse.

c) The advantages and disadvantages of majority voting rather than best base as the final classification.

d) Calculate the error for each classifier K below

e) Calculate the combined error of all K assuming they are statistically independent

f) Based on the probabilities below, do you think it is feasible that they are statistically independent?

Value	$P(K_1 = 0 C)$	$P(K_1 = 1 C)$	$P(K_2 = 0 C)$	$P(K_2 = 1 C)$	$P(K_3 = 0 C)$	$P(K_3 = 1 C)$
C=1	0.12	0.88	0.20	0.80	0.16	0.84
C=0	0.86	0.14	0.82	0.18	0.90	0.10

### Q4: PCA

Consider principle component analysis (PCA) for the 2-dimensional data below.

a) Do The PCA learning using the 2-dimentional data set in the table below. Describe the steps of your solution.

b) Sketch the data points and direction of maximal variance

- c) Compute the proportion of variance (PoV) explained by the first principal component.
- d) Find the reconstruction  $\hat{x}$  of point  $x=[4.0,7.0]^T$  with the first principle component.

$t$	$x_1^t$	$x_2^t$
1	2.0	2.0
2	3.0	4.0
3	5.0	6.0

### Q5: K-Means Clustering

Do three iterations for K-means clustering on the 2-dimensional data below. Use  $K = 2$  clusters and the initial prototype vectors (=mean vectors)  $m_1=(0.0, 2.0)$  and  $m_2=(2.0,0.0)$ . Write down calculation procedure and the cluster memberships as well as mean vectors after each iteration. Draw the data points, cluster means and cluster boundary after each iteration.

$t$	$x^t$
1	(0.0, 1.0)
2	(1.0, 2.0)
3	(4.0, 5.0)