

1. Explain the following concepts, use drawings and equations when adequate.
  - a) Describe the construction and operation principles of a synchronous generator. (Stator, rotor, windings, frequencies, etc...) (2 p.)
  - b) Draw the complete single-phase equivalent circuit of a transformer and explain what each of its component represents (2p.)
  - c) List the starting methods for a 3-phase synchronous motor. (Why they are needed?) (2 p.)
  - d) Explain the Eddy-current and Hysteresis phenomena in electrical steel (what are they? what do they affect?) (2 p.)
  - e) A 3-phase, 2-pole induction machine is fed from a 50 Hz supply. What is the rotational speed of the stator flux, rotor flux, and air gap flux in the stator reference frame (2 p.)
  - f) Explain how the power factor of a synchronous machine can be controlled, while the machine is delivering a constant active power. Draw the phasor diagram of the machine at unity power factor and lagging power factor (hint: use the terminal voltage as reference, 0 deg) (2p.).

2. In the magnetic circuit of Fig. 1, the relative permeability of the core is  $\mu_r=1200$ . All dimensions are in centimeters, and the magnetic material has a square cross section area. Neglect fringing and magnetic leakage. Use the dashed line as the average magnetic flux path.
  - a) Draw the magnetic equivalent circuit and calculate its parameters (2 p.)
  - b) Calculated the air gap flux and flux density (2 p.)
  - c) Calculate the force acting on one of the air gap ferromagnetic surfaces. (2 p.)

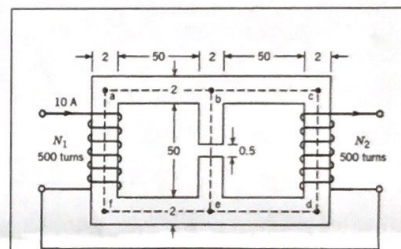


Fig. 1: Simplified inductor.

3. Explain by answering the questions bellow the tests needed to determine the parameters of the equivalent circuit of an induction machine (Fig. 2).
  - a) List and explain the connections for the tests. (2 p.)
  - b) Draw the equivalent circuits under the tests conditions. (2 p.)
  - c) What are the voltages, currents and frequencies for each test, with respect to the nominal values? (2 p.)

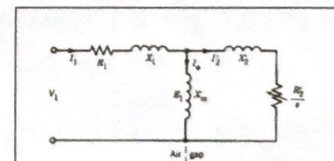


Fig. 2: Equivalent circuit of an induction machine.

4. A 2-pole DC-motor connected to 345 V supply draws 39 A current and produces 11 kW mechanical power at 1500 rpm.
  - a) Calculate the mechanical torque, and resistive losses in armature winding ( $R_a=0,8706 \Omega$ ) (2p.)
  - b) Calculate the input power of the motor and its efficiency (neglect all other losses) (2 p.)
  - c) Calculate the back electromotive force  $E_a$  when the flux factor at nominal field current is  $k_\phi=1,895 \text{ Vs/rad}$  (2 p.)

Evaluation:

Grade	Lower limit	Upper limit
0	0	13
1	14	16
2	17	19
3	20	22
4	23	26
5	27	30

Some useful formulas and drawings:

Magnetic reluctance:  $\mathfrak{R} = \frac{l}{\mu A}$

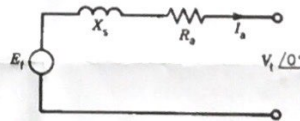
Magnetomotive force:  $F = Ni$

Force pressure:  $F_m = \frac{B_g^2}{2\mu_0}$

Speed of AC-machine:  $n = \frac{120f}{p}$  ( $p$  is the number of poles!)

Slip of induction machine:  $s = \frac{n_s - n}{n_s}$

Equivalent circuit of a synchronous generator:



Real power of a synchronous machine:  $P_{3\phi} = \frac{3|V_t||E_f|}{|X_s|} \sin \delta = P_{\max} \sin \delta$

Imaginary/Reactive power of a synchronous machine:  $Q_{3\phi} = \frac{3|V_t||E_f|}{|X_s|} \cos \delta - \frac{3|V_t|^2}{|X_s|}$

Convention: lagging reactive power positive -- > phase angle of current negative

AC active power:  $P = 3V_{ph}I_{ph} \cos \phi = \sqrt{3}VI \cos \phi$

Magnetic permeability:  $\mu = \mu_r \mu_0$ ;  $\mu_0 = 4\pi 10^{-7} \text{ Hm}^{-1}$

For an asynchronous machine, we can write the rotor resistance part as:  $\frac{R_2'}{s} = R_2' + \frac{(1-s)R_2'}{s}$

Back emf and torque of a DC machine:  $E_a = k_\phi \omega_m$ ;

$T = k_\phi I_a$