

**Question 1. Deterministic vs. Stochastic Loads**

- A. Explain the deterministic and stochastic loads for your application case (group work). What is the primary difference between how you measure deterministic vs. stochastic loads? **2p**
- B. How are the continuous probability distributions connected (e.g. Weibull, Rayleigh, Gaussian) mathematically? **2p**
- C. How can you measure the randomness of a given time history? Explain mathematically and/or graphically. **2p**

**Question 2. Mathematics of Random Process**

- A. In the assignments we mostly focused on analyzing one sample function of a random process. What assumptions allow us to use only one sample function for analyzing a random process? How would you validate these assumptions? **2p**
- B. Among the time-frequency-probability domains, which one is more helpful in assessing whether a process is narrow or broad-banded and why? How do you make a broad-banded process narrow banded? **2p**
- C. Describe the process to calculate the average and standard deviation for the position/displacement of ergodic random signal. In addition to these statistical quantities, what else do you need to derive the best fit probability distributions? **2p**

**Question 3. Environmental Loads and Responses**

- A. Describe how the random load in your application case forms (physical process). What is the idea of the scatter diagram? **2p**
- B. Explain the roles of Fourier transformation and its inverse in the context of random processes and design? **2p**
- C. What assumptions need to be valid for you to have a direct link between spectrum and probability? Explain why having a direct link is deemed useful? Was it indeed useful for your application case? **2p**

**Question 4. Assessment of design values**

- A. Explain the roles of short- and long-term assessment of random loads? How are these related? **2p**
- B. The wave spectrum [ $m^2/s$ ] and response amplitude operator [ $ton^2/m^2$ ] of the bending moment of the ship is given as:

$$W_{RAO} = \{ 0.3 \ 0.4 \ 0.5 \ 0.6 \ 0.7 \},$$

$$S_{wave} = \{ 2 \times 10^1 \ 4 \times 10^1 \ 3 \times 10^1 \ 3 \times 10^1 \ 0 \}$$

$$RAO = \{ 0 \ 2 \times 10^9 \ 4 \times 10^9 \ 3 \times 10^9 \ 0 \}$$

- Calculate maximum bending moment during 3-hour time. **2p**
- C. Calculate the  $m^{\text{th}}$  moment of load spectrum given in previous point. Select  $m$  based on last number of you student ID (0-3, 4<sup>th</sup> moment; 4-6, 6<sup>th</sup> moment; 7-9, 8<sup>th</sup> moment). **2p**