1. Let $f : \mathbb{C} \to \mathbb{C}$ be the mapping defined by condition

$$z = x + \mathrm{i}y \mapsto x^3 + \mathrm{i}(1-y)^3.$$

Find those points z in the complex plane, where f is

- (a) differentiable,
- (b) analytic.
- (c) Find the derivative $f'(z) \in \mathbb{C}$ of f at those points where it exists.
- 2. Find a Möbius mapping, that maps domain $\{z \in \mathbb{C} | |z 1| < 1\}$ to domain $\{z \in \mathbb{C} | \operatorname{Re} z > 1\}$.
- 3. Find the value of function

$$f: f(z) = \oint_{\gamma} \frac{2w^2 - w - 1}{w(w - z)e^{\pi i(w - 1)}} dw$$

at points

- (a) z = 1
- (b) z = 2
- (c) z = 4

when integration is performed along path γ that parametrizes circle

$$S(0,3) = \{ z \in \mathbb{C} | |z| = 3 \}$$

once counterclockwise.

4. Find two series in terms of powers of variable z for function f defined by conditon

$$z \mapsto \frac{1}{z(1+z^2)}.$$

Where are these series valid?