

**Appendix B. Table of Laplace transforms.**  $L(f(t)) = F(s) = \int_0^\infty f(t)e^{-st} dt$

| Nº | $f(t)$           | $F(s)$                        | Nº  | $f(t)$                        | $F(s)$  |
|----|------------------|-------------------------------|-----|-------------------------------|---|
| 1) | $1$              | $\frac{1}{s}$                 | 6)  | $e^{\alpha t} \cos \beta t$   | $\frac{s - \alpha}{(s - \alpha)^2 + \beta^2}$ |
| 2) | $\frac{t^n}{n!}$ | $\frac{1}{s^{n+1}}$           | 7)  | $e^{\alpha t} \sin \beta t$   | $\frac{\beta}{(s - \alpha)^2 + \beta^2}$      |
| 3) | $e^{\alpha t}$   | $\frac{1}{s - \alpha}$        | 8)  | $\frac{t^n}{n!} e^{\alpha t}$ | $\frac{1}{(s - \alpha)^{n+1}}$                |
| 4) | $\cos \beta t$   | $\frac{s}{s^2 + \beta^2}$     | 9)  | $\cosh \beta t$               | $\frac{s}{s^2 - \beta^2}$                     |
| 5) | $\sin \beta t$   | $\frac{\beta}{s^2 + \beta^2}$ | 10) | $\sinh \beta t$               | $\frac{\beta}{s^2 - \beta^2}$                 |

### Appendix C. Fourier transform

The Fourier transform  $F(w)$  of a function  $f(x)$  is 
$$F(w) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{+\infty} f(x) e^{-iwx} dx.$$