

5. (a) Given the signal $x_c(t) = 10 \cos(2\pi 10^8 t + 200 \cos 2\pi 10^3 t)$, what is its bandwidth in [Hz]?
 (b) What is the instantaneous frequency [Hz] of the signal $x_b(t) = 10 \cos(20\pi t + \pi t^2)$ at the time instance $t = 0$?
 (c) What is its rate of frequency change [Hz] per second?

Collection of Formulas

$$C = W_C \cdot \log_2(1 + SNR), \begin{cases} r_{\max} = 2B_T = r_b / n = r_b / \log_2(L) \\ \Rightarrow r_b = 2B_T \log_2(L), L = 2^n \end{cases}, r = n \cdot f_s$$

$$C = W_C \cdot \log_2(1 + SNR)$$

$$P_{dB} = 10 \log(P_1/P_2), P_{dB} = 20 \log(V_1/V_2), P_{dBm} = 10 \log(P_1/1mW), \frac{V_g}{V_i} = \frac{Z_g + Z_L}{Z_i}$$

$$\begin{cases} y(t) = Kx(t - t_d) \\ \Rightarrow Y(f) = F \left[y(t) = \underbrace{K \exp(-j\omega t_d)}_{H(f)} X(f) \right], \begin{cases} l = d_{\min} - 1, t = \lfloor l/2 \rfloor, R_C = k/n \leq 1 \\ d_{\min}|_{\max} = n - k + 1 \text{ (repetition codes)} \end{cases} \\ G_y(f) = |H(f)|^2 G_x(f) \text{ (= output PDF)} \end{cases}$$

$$\begin{cases} N_R = \int_{-\infty}^{\infty} (\eta/2) |H_R(f)|^2 df \\ = \int_{B_T} (\eta/2) df + \int_{B_T} (\eta/2) df = \eta B_T \end{cases} \begin{cases} P(n, k) = \binom{n}{k} \alpha^k (1 - \alpha)^{n-k} \\ \binom{n}{k} = \frac{n!}{k!(n-k)!} \end{cases}$$

$$\begin{cases} B_T = 2|D-1|W, 1 \gg D \gg 1 \\ \beta = A_m f_{\Delta} / f_m |_{A_m = 1, f_m = W} = f_{\Delta} / W \equiv D \\ B_{T,DSB} = 2W, B_{T,SSB} = W \end{cases} \begin{cases} c_n = \frac{1}{T} \int_T x(t) \exp(-j2\pi f_0 t n) dt \\ f(x) = a_0/2 + \sum_{n=1}^{\infty} a_n \cos(nx) + \sum_{n=1}^{\infty} b_n \sin(nx) \\ a_0 = \pi^{-1} \int_{-\pi}^{\pi} f(x) dx, a_n = \pi^{-1} \int_{-\pi}^{\pi} f(x) \cos(nx) dx \\ b_n = \pi^{-1} \int_{-\pi}^{\pi} f(x) \sin(nx) dx \end{cases}$$

$$\begin{cases} x_c(t) = A_C \cos(\omega_c t + \phi(t)) \\ \phi_{PM}(t) = \phi_{\Delta} x(t) \\ \phi_{FM}(t) = 2\pi f_{\Delta} \int_{t_0}^t x(\lambda) d\lambda, t \geq t_0 \end{cases} \phi(t) = \begin{cases} \frac{\phi_{\Delta} A_m}{\beta} \sin(\omega_m t), PM \\ \frac{(A_m f_{\Delta} / f_m)}{\beta} \sin(\omega_m t), FM \end{cases} \begin{cases} \gamma = S_R / (\eta W) \\ S_R / N_R = \gamma W / B_T \\ \gamma_b = E_b / N_0 \end{cases}$$

$$y(t) = \begin{cases} v_i(t) & \text{Synchronous detector} \\ A_v(t) - \bar{A}_v & \text{Envelope detector} \\ \phi_v(t) & \text{Phase detector} \\ d\phi_v(t)/dt & \text{Frequency detector} \end{cases}, \begin{cases} x_{AM}(t) = A_C [1 + \mu x_m(t)] \cos(\omega_c t) \\ x_{DSB}(t) = x_m(t) \cos(\omega_c t) \end{cases}$$