

**T-79.4302 Parallel and Distributed Systems
Examination, 14 December 2011**

Write down on every answer sheet: the name of the course, the course code, the date, your name, your student id, and your signature.

To pass the course, you also need at least 50 % of the home assignment points for Autumn 2011.

Assignment 1. Consider the following Promela model, where $Z \geq 1$ is a constant.

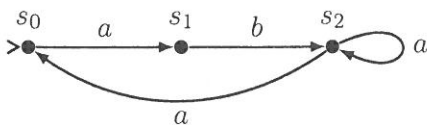
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chan bus = [Z] of { byte };
byte x = 0;
active proctype produce0() { do :: bus ! 0; od }
active proctype produce1() { do :: bus ! 1; od }
active proctype consume() {
  do
    :: bus ? x;
    :: (x == 1) -> break;
  od
}
    
```

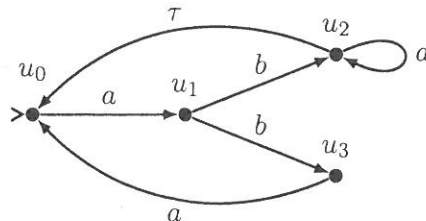
- (a) What pieces of data are needed to identify a single state of this model? Design a way to represent an arbitrary state. (2p)
- (b) Identify the sources of nondeterminism in the model. (2p)
- (c) Construct the reachability graph of the model for $Z = 1$. (4p)
- (d) List all reachable deadlock states for $Z = 2$. (2p)
- (e) How many reachable states does the model have for $Z = 4$? (2p)

Assignment 2. Given the LTSs L_1 and L_2 below, construct a deterministic finite state automaton A' that accepts the language $\Sigma_2 \setminus \text{traces}(L_2)$. See A' as an LTS L' and compute the parallel composition $P = L_1 || L'$. Use P to conclude that $L_1 \leq_{tr} L_2$. (12p)

$$L_1 : \Sigma_1 = \{a, b\}$$



$$L_2 : \Sigma_2 = \{a, b\}$$



More assignments on the second page

Assignment 3. Consider the Kripke structure $M = (S, s^0, R, L)$ with $S = \{s_0, s_1, s_2, s_3, s_4, s_5\}$, $s^0 = s_0$, $R = \{(s_0, s_1), (s_1, s_2), (s_2, s_3), (s_3, s_4), (s_4, s_2), (s_0, s_4), (s_3, s_5)\}$, and the function L is defined by $L(s_0) = L(s_1) = \{crash\}$, $L(s_2) = \{alarm\}$, $L(s_3) = \{alarm, reset\}$, and $L(s_4) = L(s_5) = \emptyset$. For each of the formulas below, check whether the formula holds in M or not. If the formula holds, give a brief explanation (max 5 lines of text) why the formula holds. If the formula does not hold, give a finite counterexample execution of M and explain why it violates the formula.

(a) $\mathbf{G} (reset \Rightarrow alarm)$ (4p)

(b) $\mathbf{G} (alarm \Rightarrow \mathbf{O} crash)$ (4p)

(c) $\mathbf{G} (alarm \Rightarrow \mathbf{Y} ((\neg reset) \mathbf{S} crash))$ (4p)

Assignment 4. Are the following statements true or false? For each statement that is true, give a brief justification. For each statement that is false, provide a counterexample that disproves the statement.

(a) There is no state s in any LTS such that there exists both a deadlock and a livelock in s . (4p)

(b) If $L_1 \leq_{tr} L_2$ and $L_2 \leq_{tr} L_1$ hold for LTSs L_1 and L_2 , then L_1 and L_2 are bisimilar. (4p)

(c) The property $\mathbf{GF} (p \Rightarrow q)$ is stuttering invariant for all atomic propositions p and q . (4p)

Please remember to give course feedback — find a link to the online form in Noppa.